

Lesson 5-3 SOLVING SYSTEMS USING ELIMINATION BY ADDITION

Key Concept Solving by Elimination

- Step 1** Write the system so like terms with the same or opposite coefficients are aligned.
- Step 2** Add or subtract the equations, eliminating one variable. Then solve the equation.
- Step 3** Substitute the value from Step 2 into one of the equations and solve for the other variable. Write the solution as an ordered pair.

EXAMPLE 1: Use elimination to solve this system of equations.

$$\begin{array}{r} 4x - 6y = 32 \\ 3x - 6y = 3 \end{array}$$

Combine like terms vertically

X's under X's
Y's under Y's
= under =

$$\begin{array}{r} 7x = 35 \\ \hline \frac{7x}{7} = \frac{35}{7} \end{array}$$

$x = 5$

find y in $4x + 6y = 32$:

$$4(5) + 6y = 32$$

$$\begin{array}{r} 20 + 6y = 32 \\ -20 \quad \downarrow \quad -20 \\ \hline 6y = 12 \end{array}$$

$$\begin{array}{r} \frac{6y}{6} = \frac{12}{6} \\ \hline y = 2 \end{array}$$

check in
 $3x - 6y = 3$
 $3(5) - 6(2) = 3$
 $15 - 12 = 3$
 $3 = 3 \checkmark$

Solution: (5, 2)

EXERCISE 1A:

$$\begin{array}{r} -4x + 3y = -3 \\ 4x - 5y = 5 \end{array}$$

$$\begin{array}{r} -2y = 2 \\ \hline \frac{-2y}{-2} = \frac{2}{-2} \end{array}$$

$y = -1$

find x in $4x - 5y = 5$:

$$4x - 5(-1) = 5$$

$$\begin{array}{r} 4x + 5 = 5 \\ \downarrow \quad -5 \quad | \quad -5 \\ \hline 4x = 0 \\ \frac{4x}{4} = \frac{0}{4} \end{array}$$

$x = 0$

check in
 $-4x + 3y = -3$
 $-4(0) + 3(-1) = -3$
 $0 - 3 = -3$
 $-3 = -3 \checkmark$

solution = (0, -1)

EXERCISE 1B:

$$\begin{array}{r} 4y + 3x = 22 \\ 3x - 4y = 14 \end{array}$$

HW

check in
 $4y + 3x = 22$
 $4(1) + 3(6) = 22$
 $4 + 18 = 22$
 $22 = 22 \checkmark$

$$\begin{array}{r} 3x + 4y = 22 \\ 3x - 4y = 14 \\ \hline \end{array}$$

$$\begin{array}{r} 6x = 36 \\ \hline \frac{6x}{6} = \frac{36}{6} \end{array}$$

$x = 6$

find y in $3x - 4y = 14$:

$$\begin{array}{r} 3(6) - 4y = 14 \\ 18 - 4y = 14 \\ -18 \quad \downarrow \quad -18 \\ \hline -4y = -4 \end{array}$$

$$\begin{array}{r} \frac{-4y}{-4} = \frac{-4}{-4} \\ \hline y = 1 \end{array}$$

solution (6, 1)

Example 2: Write and solve a system of equations

1st equation

Negative three times one number plus five times another number is -11. Three times the first number plus seven times the other number is -1. Find the numbers.

2nd equation

Negative three times one number	Plus	Five times another number	is	-11
$-3x$	+	$5y$	=	-11

Three times the first number	Plus	Seven times the other number	is	-1
$3x$	+	$7y$	=	-1

$x = \text{first number}$
 $y = \text{other number}$

Add the system to eliminate a variable:

$$\begin{array}{r} -3x + 5y = -11 \\ (+) \quad 3x + 7y = -1 \\ \hline \quad \quad 12y = -12 \end{array} \rightarrow \text{Solve for } y$$

$$y = -1$$

Replace (-1) into an original equation for "y" and solve for "x"

Top equation

$$\begin{array}{r} -3x + 5y = -11 \\ -3x + 5(-1) = -11 \rightarrow \text{Solve for } x \\ -3x - 5 = -11 \\ \quad +5 \quad +5 \\ \hline -3x \quad = -6 \\ -3 \quad -3 \\ \hline x = 2 \end{array}$$

(x,y)

Write your answer as an Ordered Pair (2, -1) What does your answer mean? The first number was 2 and the other number was -1.

Are:
 X's under X's?
 Y's under Y's?
 = under =?
 → If yes to all 3, does anything cancel out?

check in the bottom equation: $3x + 7y = -1$
 $3(2) + 7(-1) = -1$
 $6 - 7 = -1$
 $-1 = -1 \checkmark$

EXERCISE 2:

1st equation

2nd equation

The sum of two numbers is -10. Negative three times the first number minus the second number equals 2. Find the numbers. (Hint: let x = the 1st number and y = the 2nd number) Now write the system:

$$\begin{array}{r} 1x + y = -10 \quad \text{1st equation} \\ -3x - y = 2 \quad \text{2nd equation} \\ \hline -2x = -8 \quad \text{solve for } x \\ \hline -2 \quad \quad -2 \\ \hline x = 4 \end{array}$$

find y in $x+y=-10$:

$$\begin{array}{r} 4 + y = -10 \\ -4 \downarrow \quad -4 \\ \hline y = -14 \end{array}$$

check in $-3x - y = 2$:

$$\begin{aligned} -3(4) - (-14) &= 2 \\ -12 + 14 &= 2 \\ 2 &= 2 \checkmark \end{aligned}$$

Solution is (4, -14)
The first number was 4
and the second number was -14.

EXERCISE 3: Solve the system algebraically for x and y .

$$\begin{array}{r} 3x + y = 12 \\ 2x - y = 3 \\ \hline 5x = 15 \\ \hline 5 \quad \quad 5 \\ \hline x = 3 \end{array}$$

find y in $3x+y=12$:

$$\begin{array}{r} 3(3) + y = 12 \\ 9 + y = 12 \\ -9 \downarrow \quad -9 \\ \hline y = 3 \end{array}$$

check in $2x - y = 3$:

$$\begin{aligned} 2(3) - 3 &= 3 \\ 6 - 3 &= 3 \\ 3 &= 3 \checkmark \end{aligned}$$

Solution (3, 3).
The numbers are
3 and 3.